

## Mapping the Regional Transition to Cyclicity in *Clethrionomys rufocanus*: Spectral Densities and Functional Data Analysis

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**Abstract.** We study the regional transitions in dynamics of the grey-sided vole, *Clethrionomys rufocanus*, within Hokkaido, Japan. The data set consists of 225 time series of varying length (most from 23 to 31 years long) collected between 1962 and 1992 by the Forestry Agency of the Japanese Government. To see clearly how the periodic behavior changes geographically, we estimate the spectral density functions of the growth rates of all populations using a log-spline method. We subsequently apply functional data analysis to the estimated densities. The functional data analysis is, in this context, analogous to a principal component analysis applied to curves. We plot the results of the analysis on the map of Hokkaido, to reveal a clear transition from relatively stable populations in the southwest and west to populations undergoing 3-4 year cycles in the northeast and east. The degree of seasonality in the vegetation and the rodent demography appear to be strongest in the cyclic area. We briefly speculate that the destabilization of the rodent dynamics is linked to increased seasonal-forcing on the trophic interactions in which the grey-sided voles are involved.

**Key words:** biogeography, microtine cycle, population fluctuation, scale of regulation, seasonality.

### Introduction

Ecological theory predicts that changes in vital rates of individuals may lead to dramatic changes in patterns of dynamics (e.g. May 1976). Changing the population growth rate, for instance, may destabilize dynamics to induce periodic oscillations of increasing amplitude and period and eventually to become chaotic or quasiperiodic (Hastings et al. 1993). The composition of the ecological community within which a population is embedded is also predicted to affect population dynamics greatly through both direct and delayed density-dependent effects: The presence or absence of a given natural enemy may, for instance, change the dynamics of the host/prey

(Murdoch and Briggs 1996). These predictions have been shown to occur under controlled laboratory conditions (Begon et al. 1996; Dennis et al. 1997). The theory has proven more difficult to test in natural populations, not the least because dynamics of such populations appear to be resilient to manipulation (Myers and Rothman 1995). This may be due to the theory being deficient or the scale of population regulation is large relative to the scale of experimental manipulations (Bjørnstad et al. 1998). Myers and Rothman (1995) proposed that large-scaled biogeographic variation in the dynamics of natural populations might be studied with reference to large-scale differences in community composition. This utilizes observational studies of nature's own «experimentation», and may provide insights with respect to the nature of population fluctuations in free-ranging populations. The study of cycles in Northern European small rodent populations is the prime example of the use of this protocol (Hansson and Henttonen 1985a, 1988; Hanski et al. 1991; Bjørnstad et al. 1995).

Recently, we (Bjørnstad et al. 1996; Stenseth et al. 1996a) studied patterns of dynamics in the grey-sided vole in the Northern part of Hokkaido, Japan (see also Saitoh et al. 1998a). We found a cline from relatively stable to relatively variable and cyclic dynamics along an east-west gradient in this region. In this study we elaborate our earlier analyses by using 225 time series from the extensive set of monitoring data for the entire island of Hokkaido (Saitoh et al. 1998b; see also Kaneko et al. 1998). In order to do so we introduce a set of statistical methods dedicated to the description of geographic differences in stability and cyclicity.

Because time series are the most natural source of information about fluctuations, the study of geographic variation in dynamics has always hinged on long-term data. Furthermore, since the variation tends to be on a wide geographic scale, the data also has to be spatially extensive. Spatio-temporal data of this kind usually contain time series with varying length and quality. This is partly because the collection of such data tends to be demanding, and partly because the extent of the study area often changes through the course of the survey. In the following we deal with this challenge by combining recent developments in spectral analysis (Wahba 1980; Kooperberg et al. 1995) with functional data analysis (Ramsay and Silverman 1997). This allows us to investigate how the spectral density function and periodic behavior of time series varies geographically. The method is related to that previously described by Bjørnstad et al. (1996). We end the paper with a biological discussion of the ecological correlates of the geographic pattern in dynamics.

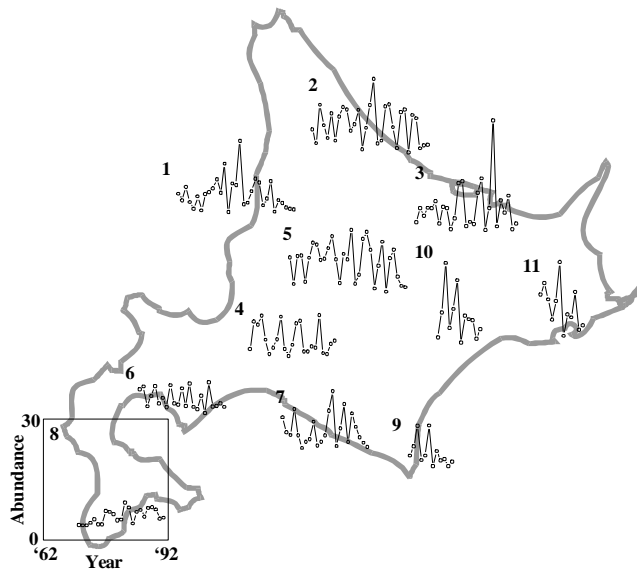


Fig. 1. The average time series for all station within each of 11 regions (see Saitoh et al. 1998a), superimposed on a map of Hokkaido. The scale is the same for all series. The first year of censusing varies between the regions but all series end in 1992.

### The data

We analyze the data on abundance of the grey-sided vole *Clethrionomys rufocanus* (Sundevall 1846) described in Saitoh et al. (1998a). The data set is comprised of 225 time series collected by the Forestry Agency of the Japan Government between 1962 and 1992. Of these, 194 series covers more than 20 years; the remaining 31 time series (from the southeastern corner of Hokkaido; i.e. East-Hidaka, Tokachi and Kushiro-Nemuro regions) are only 12 years long. The series from the northern area (the Asahikawa region) are all 31 years long, and have previously been studied in some detail (Bjørnstad et al. 1996, 1998; Stenseth et al. 1996a; Saitoh et al. 1997, 1998b). From these studies it is known that some of the populations appear to undergo regular cycles whereas others do not.

In the following we analyze the census counts standardized to 150 trap-nights as the index of abundance (see Stenseth et al. 1996a, 1997). In order to help visualize the data we also group the 225 series into 11 broad regions within which the correlation between time series is relatively high (Saitoh et al. 1998a). The average time series for each of these 11 regions are shown in Fig. 1. The most violent fluctuations are seen in the northeastern populations. The southwestern area harbors the most stable populations (see also Saitoh et al. 1998a).

### Methods

In this study we focus on short-term periodic behavior likely to be induced by ecological interactions. Long-term behavior and trends are

usually due to external forcing and anthropogenic influences requiring separate explanations (cf. Saitoh and Nakatsu 1997). To focus on the high frequency behavior we therefore study the population growth rates (the first differenced log-transformed data, Bjørnstad et al. 1996). A constant of unity was added to all counts prior to transformation.

The spectral density function,  $S(\mathbf{w})$ , is the natural tool for considering frequency properties of a process (e.g. Priestley 1981). In terms of this function the process can be decomposed into sums of sine and cosine functions of varying frequencies  $\mathbf{w}$ . The height (amplitude) of the spectral density function within a small frequency interval  $[\mathbf{w}_i, \mathbf{w}_i + \Delta\mathbf{w}_i]$  represents the proportion of the variability of the process attributable to periodic behavior with frequencies within this interval. Biogeographic variation in cyclicity implies that the spectral density of time series of abundance changes consistently across a region.

The simplest way to get an estimate of the spectral density function of a time series of length  $T$  is by calculating the *periodogram*,  $I(\mathbf{w})$ , which is proportional to the squared correlation between the time series,  $\{x_t\}$  and the sine/cosine waves of a given frequency:

$$I(\mathbf{w}) \propto \frac{1}{T} \left( \sum_{t=1}^T x_t \sin(\mathbf{w}t) \right)^2 + \frac{1}{T} \left( \sum_{t=1}^T x_t \cos(\mathbf{w}t) \right)^2. \quad (1)$$

For a discrete spectrum time series of the form

$$x_t = \sum_{j=1}^{T/2} A_j \cos(f_j t) + B_j \sin(f_j t), \quad (2)$$

where,  $\mathbf{m}$  is the mean,  $f_j$  are the discrete Fourier frequencies given by  $\{f_j = 2\pi j/T, j = 1, \dots, T/2\}$ ,  $A_j$  and  $B_j$  are Fourier coefficients, the periodogram satisfies  $I(f_j) \propto A_j^2 + B_j^2$  (the constant of proportionality depends on the exact definition used; e.g. Chatfield 1989).

Note that since the periodogram,  $I(\mathbf{w})$ , gives estimates of the spectral density function,  $S(\mathbf{w})$ , at the discrete frequencies  $\{f_j\}$ , the exact frequencies at which the spectral density is estimated depend on the length of the time series.

A noncyclic population will have a flat periodogram for the abundances. The individual amplitudes will be  $\chi^2$ -distributed under this null hypothesis. When studying the first-differenced log-abundances time series, the pattern in the amplitude is more complicated under the null (with a deficiency of low frequencies variability). There is no analytic test against this pattern. To test for significant cyclicity we therefore use a randomization test where we permute the abundances prior to calculating the first

differences and the subsequent periodograms (see Manly 1997: chapter 11). Note that in a collection of noncyclic population, the null hypothesis should be rejected in 5% of the series due to multiple testing (at a nominal 5%-level).

The dependence on series length of the frequencies at which the periodogram is estimated makes it difficult to combine information from time series of different duration. Another problem with the periodogram is that it does not provide a *consistent* estimate of the spectrum (that is, it does not converge to the true spectral density as the length of the time series increases; e.g. Wahba 1980). Therefore, it is better to work with direct estimates of the spectral density function,  $S(\mathbf{w})$ .

To obtain a consistent estimate,  $\hat{S}(\mathbf{w})$ , of the spectral density function, we make use of the following result (found in, e.g. Priestley 1981; see also Kooperberg et al. 1995). For a Gaussian process with true spectral density  $S(\mathbf{w})$ , the amplitudes  $I(f_i)$  of the periodogram are, asymptotically, independently distributed as  $S(f_i)W$ , where  $W$  is exponentially distributed (except when  $i = 0$  or  $i = T/2$ , in which case  $W$  is chi-squared distributed with one degree of freedom). Thus, on a log-scale, the variation about the true spectral density is additive with constant variance and follows the distribution of  $\log W$  (known as a Gumbel distribution). A consistent estimate of the spectral density function can thus be obtained by appropriate smoothing of the log periodogram. Natural splines provide a natural choice of basis functions for this smoothing (Wahba 1980; Kooperberg et al. 1995). In practice, we perform the smoothing by using quasilielihood assuming the variance to be proportional to the squared-mean (as for the exponential distribution) and with a log-link (Kooperberg et al. 1995; see also Hastie and Tibshirani 1990). For the 194 time series that are longer than 20 years we optimize the estimated spectral density function (optimizing the number and locations of spline knots according to the BIC criterion using the algorithm of Kooperberg et al. 1995). The 31 time series of length 12 are too short for this optimization, so we use a spline with fixed knots and 5 degrees-of-freedom (Kooperberg et al. 1995). All calculations were done in S-plus version 3.3 (Statistical Sciences 1995); the log-density estimation was done using the LSPEC library (Kooperberg et al. 1995).

Once all the spectral density functions  $\hat{S}_j(\mathbf{w})$  ( $j = 1, \dots, 225$ ) have been calculated, we have a data set composed of smooth functions from 225 different sites. Each «data-point» for further analysis is thus a curve or *function*. It is, therefore, natural to use *functional data analysis* (FDA) to describe the main types of functions (Ramsay and Silverman 1997). We want to decompose the 225 functions into a small

number of *empirical orthogonal functions* (Castro et al. 1986; Ramsay and Silverman 1997). The underlying idea is to find a small set of orthogonal functions,  $\{u_i, i = 1, \dots, p\}$ , in terms of which all of the  $n$  curves can be described well through linear combinations:

$$S_j(\mathbf{w}) \approx \sum_{k=1}^p \mathbf{b}_{jk} u_k(\mathbf{w}).$$

That is, we seek a set of principal functions which linear combinations (approximately) add up to the estimated spectral density functions. The method is analogous to a principal component analysis, but applied to functional data. The first principal orthogonal function accounts for the main axis of variation among the curves, and the second orthogonal function accounts for the subdominant axis of variation (under the constraint of orthogonality; Ramsay and Silverman 1997: chapter 6). Due to the way the calculations are done, it is usually possible to consider only a few of the orthogonal functions, which together explain most of the original variation. In the following we do the functional PCA by discretizing the curves (sampled uniformly at 101 frequencies between 0 and 0.5; Castro et al. 1986; Ramsay and Silverman 1997: chapter 6.4).

To visualize the decomposition we may examine the most important empirical orthogonal functions,  $u$ , directly. It is also illuminating to see how the overall mean function is affected by adding or subtracting a suitable multiple of each of the most important functions (Ramsay and Silverman 1997). The *scores*,  $\mathbf{b}_{jk}$ , denote the coefficients for each site,  $j$ , for each orthogonal function,  $u_k$ , that make up the linear combinations to span the spectral density. These numbers provide a classification of all sites along the principal axes of variation. Plotted on a map, these will highlight the main geographic variation in periodicity (Goodall 1954; Bjørnstad et al. 1996).

## Results

Figure 2 shows the periodograms (of the growth rates) of the 11 regional time series of vole abundance. The peaks in the northeastern and interior time series reflect multiannual 3-4 year cycles in abundance (see Fig. 1a and Bjørnstad et al. 1996). The randomization test reveals significant cyclicity with a 3.5-4.5 year period in regions 2 ( $P = 0.03$ ), 3 ( $P = 0.08$ ) and 5 ( $P = 0.02$ ). The 5.5-year cycle in region 4 is also highly significant ( $P < 0.01$ ). This time series is unusual in exhibiting a bimodal spectrum. The dynamics in the western area is aperiodic (region 1) or cyclic with a 2.5-year period (region 6 and 7; both  $P < 0.01$ ). The extreme southwest (region 8) exhibits relatively stable dynamics. The estimated spectral density functions

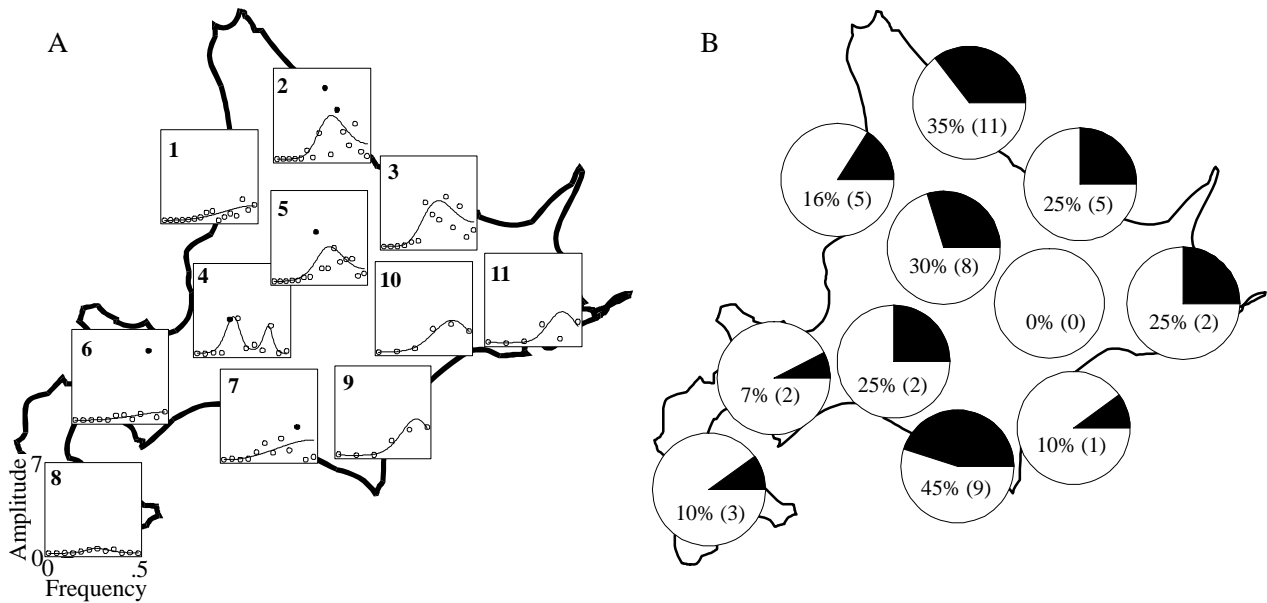


Fig. 2. A. The periodograms (dots) of the growth rates (1st differenced log-abundances) for the 11 regional averaged time series (see Fig. 1). Significant amplitudes are represented by filled symbols. The estimated spectral densities are superimposed (lines), and scaled to match the periodogram amplitudes. The spectral densities have been estimated by smoothing with the log-density method (see main text). B. The proportion (and number) of individual time series within each region that are significantly (5%) cyclic in the 3.5-4.5 year range according to the randomization test.

for the 11 regional time series are superimposed on the periodograms in Fig. 2a.

The proportion of individual time series and periodograms that harbors significant periodicity (at a nominal 5% level according to the randomization test) in the 3.5-4.5 years range (Fig. 2b), corroborates the crude spatial pattern described by the regional mean series. Around one-third of the series in the northeastern and central areas exhibit significant multiannual cycles. The proportion of such series in the western and in the southeastern area is low. Regions 6, 8, 9 and 10 have rejection rates close to that expected by multiple testing alone. It should be noted, though, that the power of these individual tests is not likely to be very high. The power furthermore hinges critically on the length of the time series. Purely statistical effects may therefore confound the ecological pattern (particularly for the very short series of regions 9-11).

To enhance the power and resolution we carry out a functional data analysis (FDA) of the spectral density functions. We concentrate on the 194 series that are long enough to apply the log-density method. The functional decomposition of these spectral densities reveals that 89% of the variation can be accounted for by three empirical orthogonal functions (Fig. 3). The four dominant functions account for 95% of the variation. It appears, however, that two or possibly three orthogonal functions suffice to span the variation in the periodic behavior. The first orthogonal function (Fig. 3a) accounts for 48% of the

variation and captures the variation in the level of high-frequency variation (and most notably in the 0.5-0.4 frequency range = 2-2.5 year range). Stations with positive scores for this function have relatively high levels of low-period variation. The second orthogonal function (Fig. 3b) accounts for 28% of the variation and represents the propensity to undergo 3.5-4.5 years cycles. The function has a trough at the frequency corresponding to a 3.7-year cycle. Negative scores of the second orthogonal function thus, crudely speaking, reflects time series with 'typical' rodent cycles. The third orthogonal function (Fig. 3c) accounts for 14% of the variation. This function will shift the periodicity downwards when negative.

Plotting the scores for each of these three functions on the map of the study area reveals a striking biogeographic pattern in population dynamics (Fig. 4). The scores of the first orthogonal function (Fig. 4a) highlight the relative stability (negative scores) of particularly the southwestern populations, but also of the coastal northwestern and coastal eastern populations. The scores of the second orthogonal functions (Fig. 4b) highlight a clearly defined region of populations that undergo multiannual cycles in abundance (negative scores). The core of this area appears to be the northeastern and interior area. But there is evidence of multiannual cycles through most of the eastern Hokkaido. There is less spatial structure in the scores of the third orthogonal function (Fig. 4c). This function may possibly reflect the orthogonality constraint inherent in the functional

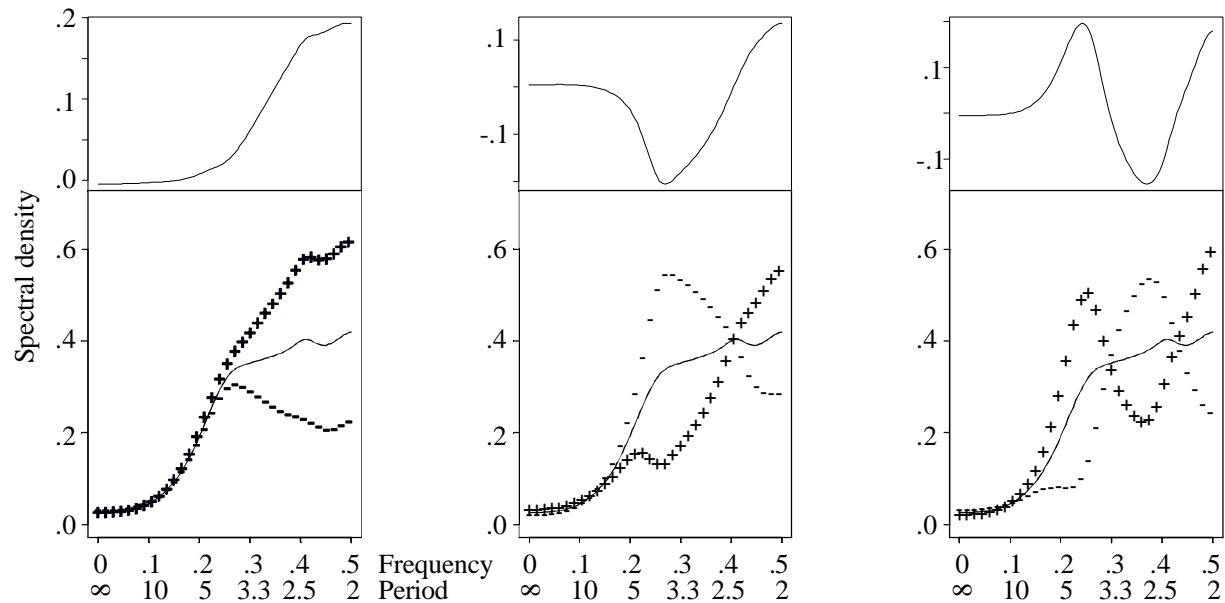


Fig. 3. The three most important orthogonal empirical functions from the FDA of the spectral densities. Top panel shows the functions themselves, and the lower panel displays the functions as positive (+) or negative (-) displacements from the mean spectral density. The 1st function captures 48%, the 2nd captures 28% and the third captures 14% of the total variation in spectral densities.

analysis more than biology. This component does, however, highlight that several of the time series around region 4 undergo cycles with period around 5 years (see also Fig. 1). The randomization tests reveal that several of these are individually significant.

Turning to the pattern in the 31 short time series in regions 9-11, the estimated spectral densities are relatively variable because only 6 frequencies are naturally evaluated in the periodogram. These 31 functions may nevertheless be decomposed in the empirical orthogonal functions from the FDA. The three dominant empirical orthogonal functions described in Fig. 3 explain most of the variation in these series (median variance explained is 88%, with inter-quartile range 68%-93%). The scores from this decomposition are given in grey symbols in Fig. 4. The pattern in these coefficients appears to follow the general geographical pattern, with indications of multiannual cyclicity in several of the populations.

## Discussion

We have introduced a method to highlight geographic transitions in population dynamics from panels of time series with heterogeneous sampling schemes. We apply this method to a large data set on abundance of the grey-sided vole of Hokkaido. We demonstrate a large-scale transition in dynamics from relatively stable or aperiodic populations in the southwest and west, to cyclic populations in the northeast and east.

Large-scaled changes in population dynamics of a species have been suggested to represent nature's own

lab experimentation (Myers and Rothman 1995). Although not generally prone to human control, such broad patterns have helped generate hypotheses for which mechanisms may underlie population cycles in a number of systems. Shepherd et al. (1988), for instance, studied outbreak patterns of the Douglas-fir tussock moth, and correlated the absence of a virus in some areas to the differences in outbreak pattern. Butler (1951) studied cycles in the colored fox in Quebec. He studied the transition from 10-year cyclicity in the boreal forest to 4-year cyclicity in the northern tundra and came up with different hypotheses for this. One was to argue that the fox is largely a side-player in these ecosystems and tracks either the 10-year cycle of the snowshoe hare or the 4-year cycle of the lemmings (but see Butler 1951 for details). Fromentin et al. (1997) demonstrated that coastal cod populations are cyclic (with a 2-3-year period) in sheltered areas and aperiodic elsewhere. They argue that age-structured interactions will give rise to cycles in abundance, but that migration and disturbances in the exposed areas are sufficiently strong to erode the cycles. Grouse populations of Scotland undergo 6-15 year cycles in abundance. Those of England undergo more violent 3-4 year cycles. The cycles have in the former case been argued to be caused by social and age-structured interactions in the former (Moss et al. 1996), but by host-parasite interaction in the latter (Dobson and Hudson 1994).

The most classical regional transition in dynamics is that seen in microtine rodents. This pattern has been carefully studied in Northern Europe (Hansson and Henttonen 1985a, 1985b, 1988; Hansson 1987;

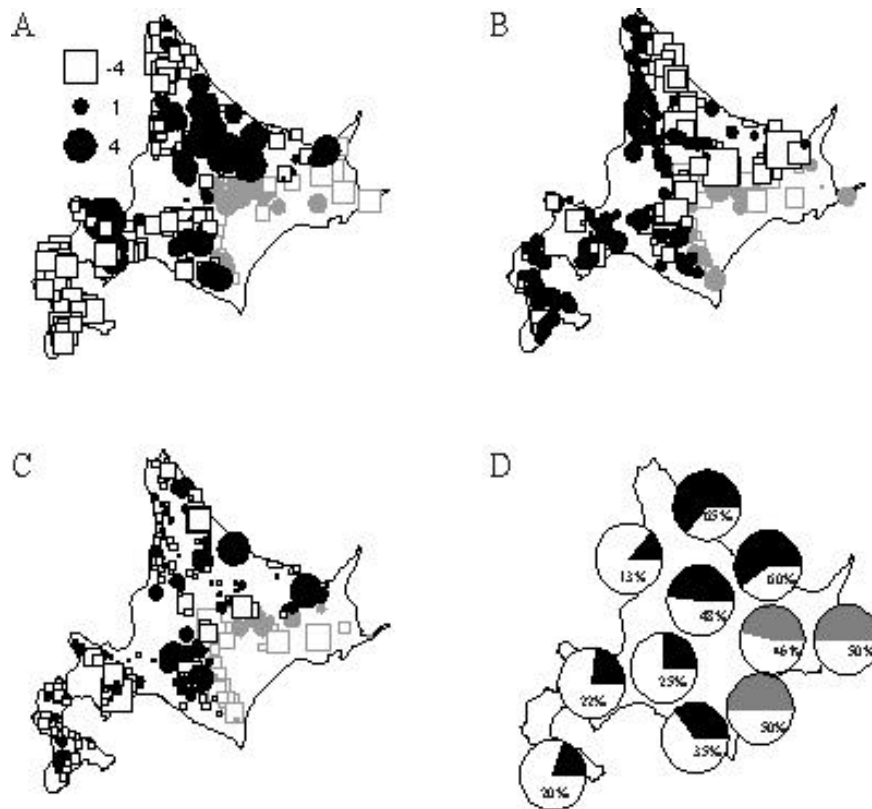


Fig. 4. Mapping of the scores for each of the 225 time series corresponding to the three most important empirical orthogonal functions (A: the first; B: the second; and C: the third orthogonal function; see Fig. 3). Filled circles represents positive scores, open squares represents negative scores. The size of the symbol represents the absolute value of the score. The symbols in black ink represent scores for density estimates that have been optimized using the log-density algorithm of Kooperberg et al. (1995). Grey symbols represents densities estimated by the fixed spline method (they were too short for optimization; see main text). D. The proportion of stations within each region that had negative score of the 2nd orthogonal function. This corresponds to the proportion of stations that exhibit a marked propensity for 3-4 cyclicity.

Henttonen et al. 1985; Hanski et al. 1991; Bjørnstad et al. 1995), and more recently in Hokkaido, Japan (Bjørnstad et al. 1996; Stenseth et al. 1996a; Saitoh et al. 1998a; this study). The pattern, although well described, still gives rise to controversies with respect to causal mechanisms (Stenseth et al. 1998a). Changing patterns of predation (Erlinge 1987; Erlinge et al. 1983; Hansson 1987; Hansson and Henttonen 1988; Hanski et al. 1991; Turchin and Hanski 1997), snow cover (Hansson and Henttonen 1985a; Hansson 1987; Bjørnstad et al. 1996), and vegetational characteristics (Hansson 1992; Jedrzejewski and Jedrzejewska 1996) have been invoked to explain the cline.

The transition in dynamics in northern European rodents is largely a latitudinal gradient. The multitude of hypotheses for the pattern is likely to reflect the fact that so many ecological variables correlate with latitude. An interesting feature of the Hokkadian pattern is that it is not a latitudinal gradient. It might therefore be easier to discern the different hypotheses in this system.

A fairly distinct region of cyclic vole dynamics in the northeastern, eastern and central area of Hokkaido is

apparent from our analysis (Fig. 4b, d; see also Saitoh et al. 1998a). The dominant hypothesis pertaining to the cyclicity of small rodents is that a key component is specialist trophic interactions (e.g. Hanski et al. 1993; Hanski and Korpimäki 1995; Stenseth et al. 1996b; Selås 1997). Little is known about differences between these areas in the composition of the community within which the grey-sided vole is embedded; More work is needed both with respect to the biogeography of enemies and food resources of the voles. According to the reviews and results presented by Kaneko et al. (1998) and Saitoh et al. (1998a) some correlates of the southwest-northeast gradient in dynamics and the biology of the voles/phenology of vegetation exist. Relative to the 'non-cyclic region', the cyclic region is colder and has a shorter plant growth-season. The breeding season of rodents is shorter (April-September vs March-October). Noncyclic populations typically exhibit a mid-summer pause in reproduction, whereas individuals of the cyclic populations typically reproduce continuously through the summer. Overall, therefore, cyclicity appears to correlate with the strength of the seasonality in the environment and the demography of rodents. Stenseth (1985) hypothesized

that shorter breeding seasons may destabilize rodent dynamics. Seasonal forcing has been demonstrated to be a key component in cyclic dynamics of childhood epidemics (e.g. Grenfell et al. 1995). Theoretically, it is also known to have important consequences for predator-prey interactions (King et al. 1996). The large-scaled biogeographic variation in the dynamics of the grey-sided vole of Hokkaido thus leads us to suggest a hypothesis for future testing (see also Saitoh et al. 1998a; Stenseth et al. 1998b): The degree of seasonal forcing on the demography (and on trophic interactions) could be the critical determinant of the stability and cyclicity of vole populations in Hokkaido. Since seasonality is a factor that is difficult to manipulate, theoretical modeling together observational studies of nature's own «experiments» - i.e. large scale geographic clines in seasonality and cyclicity - may provide the only feasible test for this hypothesis.

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